# From the Ternary Eu(Au/In)<sub>2</sub> and EuAu<sub>4</sub>(Au/In)<sub>2</sub> with Remarkable Au/ In Distributions to a New Structure Type: The Gold-Rich Eu<sub>5</sub>Au<sub>16</sub>(Au/  $\ln$ <sub>6</sub> Structure

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**S** Supporting Information

[AB](#page-8-0)STRACT: [The ternary](#page-8-0)  $Eu(Au/In)_2$  (EuAu<sub>0.46</sub>In<sub>1.54(2)</sub>) (I), EuAu<sub>4</sub>(Au/In)<sub>2</sub> (Eu- $Au_{4+x}In_{2-x}$  with  $x = 0.75(2)$  (II), 0.93(2), and 1.03(2)), and Eu<sub>5</sub>Au<sub>16</sub>(Au/In)<sub>6</sub>  $(Eu<sub>5</sub>Au<sub>17.29</sub>In<sub>4.71(3)</sub>)$  (III) have been synthesized, and their structures were characterized by single-crystal X-ray diffraction. I and II crystallize with the  $CeCu<sub>2</sub>$ -type (Pearson Symbol oI12; Imma;  $Z = 4$ ;  $a = 4.9018(4)$  Å;  $b = 7.8237(5)$  Å;  $c = 8.4457(5)$  Å) and the YbAl<sub>4</sub>Mo<sub>2</sub>-type (tI14; I4/mmm; Z = 2; a = 7.1612(7) Å; c = 5.5268(7) Å) and exhibit significant Au/In disorder. I is composed of an Au/In-mixed diamond-related host lattice encapsulating Eu atoms, while the structure of II features ribbons of distorted, squared Au<sub>8</sub> prisms enclosing Eu, Au, and In atoms. Combination of these structural motifs leads to a new structure type as observed for  $Eu<sub>5</sub>Au<sub>16</sub>(Au/In)<sub>6</sub> (Eu<sub>5</sub>Au<sub>17.29</sub>In<sub>471(3)</sub>) (oS108;$ Cmcm; Z = 4; a = 7.2283(4) Å; b = 9.0499(6) Å; c = 34.619(2) Å), which formally represents a one-dimensional intergrowth of the series EuAu<sub>2</sub>−"EuAu<sub>4</sub>In<sub>2</sub>". The site preferences of the disordered Au/In positions in II were investigated for different



hypothetical "EuAu<sub>4</sub>(Au/In)<sub>2</sub>" models using the projector-augmented wave method and indicate that these structures attempt to optimize the frequencies of the heteroatomic Au–In contacts. A chemical bonding analysis on two "EuAu<sub>3</sub>In" and "EuAu<sub>4</sub>In<sub>2</sub>" models employed the TB-LMTO-ASA method and reveals that the subtle interplay between the local atomic environments and the bond energies determines the structural and site preferences for these systems.

## **■ INTRODUCTION**

Polar metal-rich phases with gold have created excitement among scientists because of their unusual bonding patters and rich, amazing structural chemistry, most recently the remarkable phases in the A−Au−Tr/Tt systems (A = alkaline/ alkaline-earth;  $Tr/Tt =$  group 13 or 14 element).<sup>1</sup> The bonding patterns of these structures exhibit substantial 6s−5d orbital mixings of gold as a cons[e](#page-8-0)quence of relativistic effects, $1-3$  which have been observed for diverse more electron-poor intermetallics<sup>4−6</sup> as well as for quasicrystals  $(\overline{Q}Cs)$  a[nd](#page-8-0) their approximants  $(ACs)$ .<sup>7−11</sup> Valence electron concentrations (ve[cs\) a](#page-8-0)nd analyses of the band structures for these compounds utilizing density functi[onal](#page-8-0) theory (DFT)-based methods place these structures between the Zintl and (close to) the Hume− Rothery phases.<sup>5</sup> Typically, these more electron-poor intermetallic structures feature substantial Au/Tr or Au/Tt site mixing to opti[miz](#page-8-0)e the bonding for the polyanionic networks, but still, the homogeneity ranges for these structures indicate certain electronic flexibilities.<sup>12</sup>

One class of compounds is the broad family of structures with diamond-like gold net[wor](#page-8-0)ks, which are observed for five different structure types: the rhombohedral  $Sr_2Au_{6+x}Zn_{3-x}$ -type  $(R-3c)$ ,<sup>13</sup> the hexagonal SrAu<sub>4+x</sub>Al<sub>3−x</sub>-type  $(P-62m)$ ,<sup>14</sup> two independent orthorhombic structures, i.e.  $SrAu_{5+x}Al_{2-x}$ <sup>14</sup> and [BaA](#page-8-0)u<sub>5</sub>Ga<sub>2</sub>-type (*Pnma*, both structures),<sup>15</sup> a[nd](#page-8-0) the monoclinic  $Sr_2Au_{6+x}Zn_{3-x}$ -type  $(C_2/c)^{13}$  The voids wit[hin](#page-8-0) the Au host frameworks encompass triangular  $[Au, M]$ <sub>3</sub> clusters (M = Al, Zn, Ga, In, or Sn) or alkaline-earth Ae (Sr, Ba) and Eu atoms,13−<sup>18</sup> which are mutually exchanged for particular  $SrAu_{4+x}Al_{3-x}$ -type structures. All these structures can be derived from t[he](#page-8-0) [bin](#page-9-0)ary  $AAu_2$  (A = Sr, Ba, Eu)<sup>19–21</sup> to the extent that they are components of the Fibonacci series  $(\text{Au}_{12/6}\text{A})_m(\text{Au}_{12/6}\text{M}_3)_n$  (A = Sr, Ba, [Eu\) w](#page-9-0)ith AAu<sub>2</sub> for  $m =$ 1,  $n = 0$ ,  $AAu_4M_3$  for  $m = 1$ ,  $n = 1$ ,  $A_2Au_6M_3$  for  $m = 2$ ,  $n = 1$ , and  $Ba_{1.04}Au_{4.5}Ga_{2.4}$  or  $Eu_{1.1}Au_{4.4}Ga_{2.2}$  for  $m = 3$  and  $n = 2^{15}$ 

Another class of Au-rich intermetallic compounds which show certain electronic flexibilities comprises those structu[res](#page-9-0) adopting the YbAl<sub>4</sub>Mo<sub>2</sub>-type.<sup>22-26</sup> This type of structure is composed of an aluminum network encapsulating ytterbium and molybdenum atoms, [respec](#page-9-0)tively.<sup>24</sup> While previous examinations concentrated primarily on the A−Au−Tr/Tt systems, the Au-rich parts of the R−Au−[Tr/](#page-9-0)Tt phase diagrams (R = rare-earth element) have been studied to a lesser extent. <sup>27</sup>−<sup>29</sup> Initial hints of rare-earth-containing  $SrAu_{4+x}Al_{3-x}^{-15}$  and  $Sr_2Au_{6+x}Zn_{3-x}$ -type<sup>18</sup> compounds draw our in[terest](#page-9-0) to unprecedented realms of Au-rich, polar intermetallic [co](#page-9-0)mpounds in the R−Au−[Tr/](#page-9-0)Tt phase diagrams. Despite the fact that more recent research on the Eu−Au−In system has focused on its In-rich region,<sup>30–32</sup> still, there are

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<span id="page-1-0"></span>Table 1. Details of the Crystal Structure Investigations and Refinements for EuAu<sub>0.5</sub>In<sub>1.5</sub>, EuAu<sub>4.8</sub>In<sub>1.2</sub>, and Eu<sub>5</sub>Au<sub>17.3</sub>In<sub>4.7</sub>

	EuAu <sub>0.46</sub> In <sub>1.54(2)</sub> (I)	EuAu <sub>4.75</sub> In <sub>1.25(2)</sub> (II)	$Eu_5Au_{17,29}In_{4,71(3)} (III)$		
fw	419.80	1231.08	4705.95		
space group	Imma (No. 74)	$I4/mmm$ (No. 139)	Cmcm $(No. 63)$		
a, Å	4.9018(4)	7.1612(7)	7.2283(4)		
$b, \mathring{A}$	7.8237(5)		9.0499(6)		
$c, \mathring{A}$	8.4457(5) 5.5268(7)		34.619(2)		
vol., $\mathring{A}^3$	323.89(4)	283.43(7)			
Ζ	$\overline{4}$	2			
density (calcd), $g/cm3$	8.609	14.425	13.803		
$\mu$ , mm <sup>-1</sup>	50.65	138.17	129.74		
F(000)	700	999	7646		
$\theta$ range	$3.6 - 33.0$	$4.7 - 32.7$	$5.6 - 28.0$		
index ranges	$-8 \leq h \leq 9$	$-6 \le h \le 12$	$-8 \leq h \leq 8$		
	$-14 \le k \le 14$	$-11 \le k \le 11$	$-11 \le k \le 11$		
	$-14 \le l \le 15$	$-9 \le l \le 9$	$-42 \le l \le 42$		
no. of reflns collected	3617	2054	10702		
no. of independent reflns/ $R_{\text{int}}$	596/0.066	238/0.068	1233/0.154		
no. of reflns with $I > 2\sigma(I)/R_{\sigma}$	456/0.043 196/0.035		792/0.084		
refinement method	full-matrix least-squares on $F^2$				
data/restraints/parameter	596/0/13	238/0/11	1233/0/77		
goodness-of-fit on $F^2$	1.04	1.11	1.01		
final R indices $[F^2 > 2\sigma(F^2)]$	$R_1 = 0.035$ ; $wR_2 = 0.069$	$R_1 = 0.026$ ; $wR_2 = 0.049$	$R_1 = 0.044$ ; $wR_2 = 0.075$		
R indices (all data)	$R_1 = 0.053$ ; $wR_2 = 0.077$	$R_1 = 0.035$ ; $wR_2 = 0.051$	$R_1 = 0.086$ ; $wR_2 = 0.090$		
largest diff. peak and hole, $e^-/\AA$ <sup>3</sup>	5.12 and $-4.16$	2.55 and $-2.30$	4.59 and $-3.89$		

barely any reports regarding its Au-rich (more electron-poor) part.<sup>33</sup> Therefore, we present and discuss the results of the initial explorations for the Au-rich part of the Eu−Au−In syst[em](#page-9-0), which yielded the intermetallic compounds Eu-Au<sub>0.5</sub>In<sub>1.5</sub>, EuAu<sub>4+x</sub>In<sub>2−x</sub> (x = 0.8−1.0), and Eu<sub>5</sub>Au<sub>17.3</sub>In<sub>4.7</sub> with a new structure type for the last composition.

## **EXPERIMENTAL TECHNIQUES**

Syntheses. Gold pieces (99.999%, BASF), filings of europium (99.99%, Ames Laboratory), indium and gallium ingots (99.999% Alfa Aesar) were used as starting materials and stored and handled under dry argon atmosphere in a glovebox ( $H<sub>2</sub>O < 0.1$  ppmv). The Eu filings were produced from large ingots, which were mechanically polished prior to each use. Loads of ∼200−300 mg total were weighed in precleaned, one-side arc-welded tantalum tubes, which were closed inside a glovebox, arc welded on the other end, and jacketed by evacuated Schlenk flasks. The products were obtained using the following temperature programs. EuAu $_{0.5}$ In<sub>1.5</sub>: heat to 800 °C within 4 h, keep that temperature for 12 h, cool to 300 °C with 10 °C/h, and anneal at this temperature for 60 h. EuAu<sub>4+x</sub>In<sub>2-x</sub> (x = 0.8) and Eu<sub>5</sub>Au<sub>17.3</sub>In<sub>4.7</sub>: heat to 800 °C in 4 h, keep the temperature for 12 h, slowly cool to 300 °C (2 °C/h), anneal at this temperature for 3 days, and quench in water. Single crystals obtained from samples with loads corresponding to hypothetical compositions of "Eu<sub>2</sub>Au<sub>7</sub>In<sub>2</sub>" and "Eu<sub>1</sub>Au<sub>5</sub>In<sub>1</sub>" (Supporting Information; Table S1) pointed to a narrow solid solution for EuAu<sub>4+x</sub>In<sub>2−x</sub> (x = 0.8−1.0). The products appeared as gray powders with silver crystals of polyhedral shapes and metallic luster and we[re stable in air in accord](#page-8-0) with recently reported Au-rich compounds.15,16 Analogous reactions in the Eu−Au−Ga system yielded a rhombohedral  $Sr_2Au_{6+x}Zn_{3-x}$ -type<sup>13</sup> phase (Eu<sub>2</sub>Au<sub>6.1</sub>Ga<sub>2.9</sub>; R-3c;  $a = 8.411(5)$  $a = 8.411(5)$  $a = 8.411(5)$  Å;  $c = 21.830(13)$  Å, see Supporting Information) or hexagonal  $SrAu_{1,t+x}Al_{3-x}$ -type<sup>14</sup> compo[und](#page-8-0)s, which have been reported elsewhere.<sup>1</sup>

X-ray Studies. All samples [w](#page-8-0)ere che[cked for purity through](#page-8-0) detailed phase anal[yse](#page-9-0)s of sets of powder X-ray diffraction data, which were collected on STOE STADI P diffractometers equipped with a STOE image plate and DECTRIS MYTHEN 1K detectors (Cu K<sub>α1</sub>;  $\lambda$  $= 1.54059$  Å) at room temperature. For the measurement the samples were dispersed on Mylar sheets with grease and placed between split aluminum rings or sealed in capillaries. Data and phase analyses were carried out with the WinXPow software package.<sup>34</sup> Detailed phase analyses of the powder patterns revealed that  $EuAu_{4+x}In_{2-x}$  (x = 0.75(2) (II), 0.93(2), and 1.03(2)) were obtai[ne](#page-9-0)d as high-yield products in competition with  $Eu_5Au_{17,3}In_{4.7}$  (III), while  $EuAu_{0.5}In_{1.5}$ (I) was accompanied by the previously reported  $EuAuIn<sup>35</sup>$  (see Supporting Information).

Single crystals were selected from the bulk samples, fixed [on](#page-9-0) glass fibers with grease, and subsequently transferred to a Bruker APEX CCD diff[ractometer](#page-8-0) [\(Br](#page-8-0)uker, Inc.; Madison, WI). Sets of single-crystal X-ray intensity data were collected in  $\varphi$ - and  $\omega$ -scan modes at room temperature ( $\sim$ 296 K) with Mo K $\alpha$  radiation ( $\lambda$  = 0.71073 Å) and exposures of 15 s/frame. The raw intensity data were integrated utilizing the SAINT program within the SMART software suite,<sup>36</sup> while the program SADABS<sup>37</sup> was employed for empirical absorption corrections.

Checking the intensi[ty](#page-9-0) data sets for extinction conditions [wit](#page-9-0)h the XPREP algorithms in the SHELXTL suite<sup>38</sup> and examination of the  $E^2$ -1 statistics lead to the assignment of the centrosymmetric space groups Imma (No. 74), I4/mmm (No. 139)[, a](#page-9-0)nd Cmcm (No. 63) for EuAu<sub>0.46</sub>In<sub>1.54(2)</sub> (I), EuAu<sub>4+x</sub>In<sub>2−x</sub> (x = 0.75(2) (II), 0.93(2), and 1.03(2)), and  $\mathrm{Eu}_{5}\mathrm{Au}_{17.29}\mathrm{In}_{4.71(3)}$  (III), respectively. All structures were solved using direct methods (SHELXS-2013) and refined on  $F^2$  in fullmatrix least-squares including anisotropic atomic displacement parameters (SHELXL-2013).<sup>39</sup> Initial refinements of the  $8h$  sites in I and the 4d positions in II with the scattering factor of indium lead to too small displacement para[met](#page-9-0)ers for these sites, and close inspection of the Fourier maps for I and II indicated higher electron densities on these sites; however, subsequent refinements with the scattering factors of gold resulted in too large anisotropic atomic displacement parameters for the 8h sites in I and the 4d positions in II. Accordingly, mixed Au/In occupancies were introduced for these sites, and approaches to refine them with the same as well as different positional parameters for both gold and indium preceded to more reasonable anisotropic atomic displacement parameters for the refinements with the common Au/In positions. Analogous examinations of the 16h and 8f positions for the orthorhombic structure of III indicated the presence of mixed Au/In occupancies for the latter sites. Therefore, mixed Au/In occupancies were assigned on three 8f positions in the structure of III, which was refined to the composition

<span id="page-2-0"></span>Table 2. Atomic Positions and Equivalent Isotropic Displacement Parameters for  $EuAu_{0.46}In_{1.54(2)}$ ,  $EuAu_{4.75}In_{1.25(2)}$ , and  $Eu_5Au_{17,29}In_{4.71(3)}$ 

atom	position	$\boldsymbol{\mathcal{X}}$	$\mathcal{Y}$	$\boldsymbol{z}$	$U_{\rm iso}/U_{\rm eq}$ , Å <sup>2</sup>	Occ. $(<1)$		
$EuAu_{0.46}In_{1.54(2)}$								
Eu1	4e	$\boldsymbol{0}$	1/4	0.5418(1)	0.0170(2)			
Au2/In2	8h	$\boldsymbol{0}$	0.0485(1)	0.1637(1)	0.0181(2)	0.23(1)/0.77(1)		
EuAu <sub>4.75</sub> In <sub>1.25(2)</sub>								
Au1	8h	0.3059(1)	0.3059(1)	$\mathbf{0}$	0.0129(2)			
Eu2	2a	$\mathbf{0}$	$\mathbf{0}$	$\mathbf{0}$	0.0112(3)			
Au3/In3	4d	$\boldsymbol{0}$	1/2	1/4	0.0156(4)	0.37(1)/0.63(1)		
			$Eu5$					
Au1	16h	0.1933(2)	0.3090(1)	0.4620(1)	0.0108(3)			
Au2	16h	0.1975(2)	0.4228(1)	0.2901(1)	0.0089(3)			
Au3	16h	0.1931(2)	0.0630(1)	0.4136(1)	0.0108(3)			
Au4	16h	0.3064(2)	0.1765(1)	0.3367(1)	0.0115(3)			
Au5/In5	8f	$\mathbf{0}$	0.4057(3)	0.5319(1)	0.0085(10)	0.20(2)/0.80(2)		
Au6/In6	$8\!$	1/2	0.2846(3)	0.4045(1)	0.0119(11)	0.37(2)/0.63(2)		
Au7/In7	8f	1/2	0.4833(4)	0.3395(1)	0.0165(14)	0.07(2)/0.93(2)		
Eu8	4a	1/2	1/2	1/2	0.0091(7)			
Eu9	8f	$\mathbf{0}$	0.3703(3)	0.3755(1)	0.0093(6)			
Eu10	4c	$\boldsymbol{0}$	0.7087(4)	1/4	0.0065(7)			
Eu11	4c	$\boldsymbol{0}$	0.1472(4)	1/4	0.0101(8)			



Figure 1. Representation (a) of the unit cell of I: Au and In atoms form hexagons in chair conformations within the ac plane (b). (c) View on the unit cell of II: each europium atom is enclosed by 12 Au and 8 M atoms, while the gold network may be depicted as mutually perpendicular gold hexagons in boot conformations (d).

 $\mathrm{Eu}_{5}\mathrm{Au}_{17.29}\mathrm{In}_{4.71(3)}$  for the selected single crystal. The PLATON software package<sup>40</sup> was employed to check the symmetries of the refined structures, and no higher symmetries were identified. With these settings the  $R_1$  $R_1$  values converged to less than 4.36% (Table 1). Details of the data collection and refinement parameters for I, II, and III are provided in Table 1, whereas atomic positions ar[e listed i](#page-1-0)n Table 2.

Computational Details. Electronic structure calculations were undertaken for hypothetical EuAu<sub>4</sub>(Au/In)<sub>2</sub> (II) models representing the compositions "EuAu<sub>4</sub>In<sub>2</sub>" and "EuAu<sub>5</sub>In" (Figure 3) to identify the site preferences in the tetragonal structures. The "EuAu<sub>4</sub>In<sub>2</sub>" model differs from the experimentally determined tetragonal EuAu<sub>4+x</sub>In<sub>2-x</sub> structures ( $x = 0.8 - 1.0$ ) through full indium [occupatio](#page-5-0)n of the 4*d* site, while in the "EuAu<sub>5</sub>In" models indium atoms reside on both the 8h and 4d sites. Full structural optimizations of all models and band structure calculations were carried out using the projector-augmented wave (PAW) method of Blöchl<sup>41</sup> as implanted in the Vienna ab initio Simulation Package (VASP) by Kresse and Joubert.<sup>42-46</sup> Correlation and exchange were described b[y th](#page-9-0)e general gradient approximation of Perdew, Burke, and Enzerhof (GGA−PBE),<sup>47</sup> while [startin](#page-9-0)g meshes of  $4 \times 4 \times 4$  up to  $8 \times 8 \times 8$  k points were employed to sample the first Brillouin zone for reciprocal space integrat[ion](#page-9-0)s. The cutoff energy of the plane wave basis sets was set 500 eV, and full optimizations were accomplished until the energy difference between two iterative steps fell below  $10^{-7}$  eV/cell. An effective on-site Coulomb interaction term  $(U<sub>eff</sub> = 3 eV)$  was included in the Kohn–Sham Hamiltonian to account for the strong correlations within the Eu 4f states.

A chemical bonding analysis on all models was completed based on the integrated values of the crystal orbital Hamilton populations (COHP), which were obtained through the tight-binding linearmuffin-tin-orbital (TB-LMTO) method with the atomic sphere approximation (ASA) using the Stuttgart code.<sup>48,49</sup> In particular, the off-site projected density of states are weighted by the corresponding Hamilton matrix elements to determine bon[ding](#page-9-0) and antibonding states.<sup>50</sup> The optimized structural parameters of the models were obtained from the VASP computations and used as starting points for the T[B-](#page-9-0)LMTO-based electronic structure calculations. The Wigner− Seitz (WS) radii were generated automatically, and empty spheres (ES) were included to achieve an optimal approximation of full potentials. The basis set employed the following orbitals (downfolded<sup>51</sup> orbitals in parentheses): Au-6s/-6p/-5d/(-5f); Eu-6s/(-6p)/-5d; In-5s/-5p/(-5d)/(-4f). The corresponding WS radii (Angstroms) were [as](#page-9-0) follows: Au, 2.91−3.13; Eu 3.49−3.72; In, 3.02−3.14. On the basis of the VASP computations the Eu 4f states are strongly localized and, hence, treated as core-like states in the TB-LMTO-based calculations, which is in accord with recently reported results on R-containing compounds.<sup>52–54</sup> Reciprocal space integrations were completed with the tetrahedron method<sup>55</sup> employing  $24 \times 24 \times 24$ ,  $24 \times 24 \times 24$  $24 \times 24 \times 24$ ,  $24 \times 24 \times 24$ ,  $12 \times 6 \times 12$  $12 \times 6 \times 12$ , and  $12 \times 12 \times 6$  k-point sets for the "Eu[Au](#page-9-0)<sub>4</sub>In<sub>2</sub>", "EuAu<sub>5</sub>In-1", "EuAu<sub>5</sub>In-2", "EuAu<sub>5</sub>In-3", and "EuAu5In-4" models, respectively. Plots of the DOS and −COHP curves are shown in Figure 4, while the integrated values of the −COHP curves (ICOHP) may be extracted from the Supporting Information (Tables S3−[S6\).](#page-6-0)

## ■ RESULTS AND DISCUSSION

[More](#page-8-0) [recen](#page-8-0)t investigations of the Au-rich part of the Eu−Au− Tr (Tr = Al, Ga) systems have resulted in the identification of rhombohedral  $Sr_2Au_{6+x}Zn_{3-x}$ -type<sup>13,18</sup> (Table S1, Supporting Information) or hexagonal  $SrAu_{4+x}Al_{3-x}$ -type<sup>14,15</sup> compounds. Initial examinations of the Eu-po[or](#page-8-0) [reg](#page-9-0)ions (<33 a[t.%\) for the](#page-8-0) [correspondin](#page-8-0)g Eu−Au−In system lead to th[e d](#page-8-0)[isc](#page-9-0)overy of the Au-rich EuAu<sub>4+x</sub>In<sub>2−x</sub> (x = 0.75(2) (II)) and Eu<sub>5</sub>Au<sub>17.29</sub>In<sub>4.71(3)</sub> (III), which were detected at the same composition "Eu<sub>2</sub>Au<sub>7</sub>In<sub>2</sub>". Furthermore, the ternary EuAu<sub>0.46</sub>In<sub>1.54(2)</sub> (I) was also found at this composition. Subsequent reactions of samples loaded as "EuAu<sub>5</sub>In" produced high yields of EuAu<sub>4+x</sub>In<sub>2−x</sub> (x = 0.8−1.0; Figure S3, Supporting Information), while loadings of "EuAu<sub>4</sub>In<sub>2</sub>" uncovered the possibility of Tsai-type quasicrystals and their approxi[mants in this system.](#page-8-0)

**Crystal Structures.** The structure of  $\text{EuAu}_{0.46}\text{In}_{1.54(2)}$  (I) is [deriv](#page-8-0)ed from the binary EuAu<sub>2</sub> (Imma; No. 74; CeCu<sub>2</sub>-type<sup>56</sup>) through partial indium substitution on the gold sites (Wyckoff position  $8h$ ).<sup>21</sup> In particular, this structure features pucke[red](#page-9-0) sheets of gold/indium-mixed (M) hexagons adopting chairlike conformatio[ns](#page-9-0) within the ac plane. The M−M distances are short  $(2.851(1)-2.868(1)$  Å) within the M<sub>6</sub> rings and range from  $3.152(1)$  to  $4.671(1)$  Å between the M hexagons sandwiching the Eu host atoms (Wyckoff position  $4e$ ). Accordingly, each europium atom is enclosed by 12 M atoms forming condensed Eu@ $M_{12/6}$  cages (Figure 1). Note that the structure of I crystallizes with the  $CeCu<sub>2</sub>$ <sup>56</sup> rather than the

CaIn<sub>2</sub>-type (P6<sub>3</sub>/mmc; No. 194), which is adopted by the binary  $\text{Euln}_2$ .<sup>57</sup> Alike Au/In distributions have also been observed for the polyanionic networks of the previously reported  $BaAu_{0.4}In_{1.6}^{58}$  and  $GdAu_{0.4}In_{1.6}^{59}$  The structure of the barium-containing compound represents a substitutional solution of gold in  $\text{Baln}_2^{\delta 0}$  (CeCu<sub>2</sub>-ty[pe](#page-9-0)<sup>56</sup>), while the M network of  $GdAu_{0.4}In_{1.6} (Caln_2-type^{57})$  assembles a hexagonal diamond-like substructure [as](#page-9-0) observed for [th](#page-9-0)e rhombohedral  $Eu_2Au_{6,1}Ga_{2,9}$  (see Supporting Infor[ma](#page-9-0)tion).

Alloys in the series EuAu<sub>4+x</sub>In<sub>2−x</sub> ( $x = 0.8-1.0$ ) adopt the YbAl<sub>4</sub>Mo<sub>2</sub>-type of structure  $(I4/mmm;$  No. 139)<sup>24</sup> and are composed of gold networks encapsulating Eu and M ( $M = Au$ ) [I](#page-9-0)n) atoms, respectively. The structures of the EuAu<sub>4+x</sub>In<sub>2−x</sub> (x = 0.8−1.0) series show alike structural features, and the indiumrichest representative,  $EuAu_{4.75}In_{1.25(2)}$ , was selected for further structural analysis. Gold atoms residing on Wyckoff position 8h form mutually perpendicular, puckered layers of  $Au<sub>6</sub>$  hexagons, which adopt boot-like conformations within the ac and bc planes (Figure 1). The Au−Au distances along the apexes of the hexagons  $(2.986(1)$  Å) are longer than the Au–Au separations  $(2.780(1)$  Å) that encompass the bases of the  $Au<sub>6</sub>$  circles and, furthermore, the  $Au<sub>4</sub>$  squares parallel to the ab plane. Alternatively, the Au substructure can be depicted as distorted, squared  $Au_8$  prisms that are condensed via common faces to construct ribbons along (001). Each europium atom (Wyckoff position  $2a$ ) is enclosed by two face-sharing  $Au_8$ prisms with eight M atoms (Wyckoff position 4d) capping their faces along the c axis (Figure S5, Supporting Information). Accordingly, each europium atom is coordinated by 12 Au and eight M atoms, guiding to a coordina[tion number of 20 for Eu](#page-8-0). Similarly, each M atom occupies a center of a distorted, squared Au<sub>8</sub> prisms with Au–M distances of 2.939(1) Å. Additionally, the  $M@Au<sub>8</sub>$  cages are bicapped by the endohedral M atoms of the nearest neighboring  $Au_8$  prisms leading to M–M contacts of  $2.763(1)$  Å within the ribbons.

The nearest structural analogues come from the previously reported SrAu<sub>4.8</sub>In<sub>1.2</sub><sup>25</sup> and EuAu<sub>4.8</sub>Cd<sub>1.2</sub><sup>26</sup> (YbAl<sub>4</sub>Mo<sub>2</sub>-type;<sup>24</sup> both structures). The Sr-containing structure features close M− M contacts ( $M = Au/In$  $M = Au/In$  $M = Au/In$ ; 2.764(1) Å) [wit](#page-9-0)hin the chains a[nd](#page-9-0) Au–Au distances of 2.782(1) Å for the Au<sub>4</sub> squares, while the M−M distances (here  $M = Au/Cd$ ) are 2.730(1) Å within the chains in the structure of  $EuAu_{4,8}Cd_{1,2}$ . A clear difference between SrAu<sub>4.8</sub>In<sub>1.2</sub> and the structures of EuAu<sub>4+x</sub>In<sub>2−x</sub> (x =  $0.93(2)$ ,  $1.03(2)$ ; Supporting Information) arises from the distribution of the Au and In atoms, as the mixed 4d sites are occupied by about [or even more than 50 ato](#page-8-0)m % Au in the Eucontaining compounds. Comparatively, phase analytical studies based on powder X-ray diffraction data for the Eu−Au−Cd systems pointed to a substitutional homogeneity range of  $0 \leq x$  $\leq$  1 for EuAu<sub>4+x</sub>Cd<sub>2-x</sub><sup>26</sup> yet, a "EuAu<sub>4</sub>In<sub>2</sub>" composition, which shows no Au/In mixing for the 4d sites, has not been observed for this system. Previ[ous](#page-9-0) investigations in the Ce−Mn−Cu<sup>61</sup> and La-Ag-Mg<sup>62</sup> systems indicated that the ranges of compositions for solid solutions with the YbAl<sub>4</sub>Mo<sub>2</sub> type [of](#page-9-0) structure partiall[y](#page-9-0) overlap with those of different structure types. For instance, an increase of the Ag content in LaAg<sub>4+x</sub>Mg<sub>2-x</sub> going from  $x = 0.4$  to  $x = 0.9$  leads to a different chemical occupation of the relative crystallographic sites and an order−disorder transformation from the  $YbAl<sub>4</sub>Mo<sub>2</sub>$ - (I4/mmm; No. 139) to the LaAg<sub>5</sub>Mg-type (P4/  $nmm$ ; No.  $129)$ .<sup>62</sup> Such polymorphism could not be encountered for the structures of EuAu<sub>4+x</sub>In<sub>2−x</sub> (x = 0.8−1.0), as close inspection [o](#page-9-0)f the extinction conditions for the X-ray

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Figure 2. Representatives of the linear, inhomogeneous intergrowth series EuAu<sub>2</sub><sup>21</sup> (13; a)−"EuAu<sub>4+x</sub>In<sub>2−x</sub>" (13; b; Eu, dark gray; Au, yellow; M, blue; In, green): the monoclinic  $Eu_{5}Au_{17,7}In_{4,3}^{33}(C2/m; c)$  and orthorhombic  $Eu_{5}Au_{17,3}In_{4,7}$  (Cmcm; d) formally represent one-dimensional intergrowths of the series EuAu<sub>2</sub>−"EuAu<sub>4+x</sub>In<sub>2−x</sub>". Full indium occupations of the disordered 4*d,* 4*i,* and 8*f* sites for EuAu<sub>4.8</sub>In<sub>1.2</sub>, Eu<sub>5</sub>Au<sub>17.7</sub>In<sub>4.3</sub>, and  $Eu_{5}Au_{17,3}In_{4,7}$ , respectively, lead to the compositi[on](#page-9-0)s "EuAu<sub>4</sub>In<sub>2</sub>" and "Eu<sub>5</sub>Au<sub>16</sub>In<sub>6</sub>", which point to the presence of an intergrowth series. The twodimensional parent segments EuAu<sub>2</sub> and "EuAu<sub>4+x</sub>In<sub>2−x</sub>" form infinite slabs stacked along (001) for both intergrowths. Note the dissimilar stacking between the monoclinic (c) and the orthorhombic (d) structures.

intensity data sets as well as  $E^2$ -1 statistics for these structures clearly pointed to the space group I4/mmm. It is worth noting that mixed occupancies occur on the 4d rather than the 8h sites in the crystal structures of the  $YbAl<sub>4</sub>Mo<sub>2</sub>$ -type ternary phases with substitutional homogeneity ranges;25,26,61−<sup>63</sup> however, conclusive hints accounting for this preference have not been provided. Electronic structure calcula[tions](#page-9-0) [on](#page-9-0) different "EuAu<sub>5</sub>In" models will provide insight into the origin for this site preference (see Coloring and Electronic Structure).

 $Eu<sub>5</sub>Au<sub>17.29</sub>In<sub>4.71(3)</sub> (III) crystals in its own structure type$ (Cmcm; No. 63) an[d formally resembles a one-dimensi](#page-5-0)onal (or linear) intergrowth of "EuAu<sub>4+x</sub>In<sub>2−x</sub>"-related (the term "EuAu<sub>4+x</sub>In<sub>2−x</sub>" refers to segments showing the similar structural features as observed for EuAu<sub>4+x</sub>In<sub>2−x</sub> (x = 0.8 −1.0)) and EuAu2-related (two-dimensional) slabs. Strictly speaking, evaluation of a direct structural relationship between EuAu<sub>4.75</sub>In<sub>1.25(2)</sub> and Eu<sub>5</sub>Au<sub>17.29</sub>In<sub>4.71(3)</sub> is set hurdles by the dissimilar occupancies of the disordered positions in II and III; however, a topological analysis of all structures with an approximation of full indium occupancies for the mixed Au/ In 4d and 8f positions in II and III, respectively, guides to a structural relationship akin to a linear inhomogeneous intergrowth from  $EuAu<sub>2</sub>$  and II to III.

The orthorhombic structure contains three independent M sites (Wyckoff positions  $8f$ ,  $8f$ ,  $8f$ ) residing in the centers of the distorted, squared Au<sub>8</sub> prisms. The contacts between two endohedral M atoms (2.790(4)−2.879(4) Å) are slightly larger than those observed for II and suggest coordination environments of eight Au and two M atoms for the four M atoms within one ribbon (Figure S6, Supporting Information); however, the  $M(\partial A)$  cages at the ends of each ribbon are capped by one M and one Eu atom  $(d(Eu-M) = 3.436(4)$  Å). In addition to the intercalation of the EuAu<sub>2</sub>-fashioned slabs, the orthorhombic structure comprises four independent europium positions. Two europium sites (Wyckoff positions 4c, 4c) are located in the  $Au_{12}$  cages of the EuAu<sub>2</sub> segments, whereas two other europium sites (Wyckoff position 4a and 8f) are enclosed by face-sharing  $Au_8$  prisms (Figure S6, Supporting Information). The Eu atoms in the centers of the "EuAu<sub>4+x</sub>In<sub>2−x</sub>"-related slabs (Wyckoff position 4*a*[\) are](#page-8-0) [surrounded b](#page-8-0)y 12 Au and eight M atoms in accord with the Eu coordination spheres in II, while the europium atoms residing on Wyckoff position 8f possess  $(12Au + 7M)$ coordination environments. In contrast to the tetragonal structure the bases of the  $Au_8$  prisms show slight distortions, as they range from  $2.785(2)$  to  $2.794(2)$  Å within and from 2.799(2) to 2.856(2) Å at the edges of the "EuAu<sub>4+x</sub>In<sub>2−x</sub>" segments. The Au–Au contacts in and between the  $Au<sub>6</sub>$  rings of the EuAu<sub>2</sub> layers scale from 2.776(2) to 2.861(2) Å, in fair agreement with those observed for  $\text{EuAu}_2^{21}$  (2.714–2.917 Å).

The nearest structural analogue comes from the previously reported Eu<sub>5</sub>Au<sub>17.7</sub>In<sub>4.3</sub> (C2/m; No. 1[2\),](#page-9-0)<sup>33</sup> which is also composed of EuAu<sub>2</sub>- and "EuAu<sub>4+x</sub>In<sub>2−x</sub>" parental segments. Although a strict structural comparison betw[ee](#page-9-0)n II, III, and the monoclinic structure cannot be accomplished due to the dissimilar disorder of the M positions, a topological analysis of the segments for  $Eu_5Au_{17,3}In_{4,7}$  and  $Eu_5Au_{17,7}In_{4,3}$  implies that these structures resemble one-dimensional (or linear) intergrowths in the series EuAu<sub>2</sub>−"EuAu<sub>4+x</sub>In<sub>2−x</sub>" based on the approximations of full indium occupancies for the disordered M sites in these structures. In particular, the orthorhombic  $Eu<sub>5</sub>Au<sub>17,3</sub>In<sub>4,7</sub>$  and the monoclinic  $Eu<sub>5</sub>Au<sub>17,7</sub>In<sub>4,3</sub>$  both feature sequences of three succeeding "EuAu<sub>4+x</sub>In<sub>2−x</sub>" segments (3<sup>6</sup><sub>1</sub>) and one EuAu<sub>2</sub> slab  $(1^3_2)$ , which are stacked alternately along (001) in accordance with the formulas  $(3_1^61_2^3)$  and  $(3_1^61_2^3)_2$  for the monoclinic and orthorhombic structures, respectively (Figure 2). The superscript indexes 3 and 6 represent mirror planes and two-folded axes, respectively, that are arranged

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Figure 3. Coloring models of hypothetical "EuAu<sub>5</sub>In" structures: gold and indium sites are represented by the gold and green atoms, respectively. In models 1 and 2 (top) the indium atoms reside on the 8h sites, while the 4d positions are occupied by indium in models 3 and 4 (bottom). From the total energies of the different schemes it is clear that there is a site preference for the 4d sites. Placing In on the 4d sites surrounded by 10 nearest neighboring gold atoms leads to the maximum possible number of 10 heteroatomic Au−In contacts per In. Because each model comprises 26 M−M contacts/fu, the maximal percentage of the Au-In bonds to all M-M contacts is reached for 38.46%, which is achieved for "EuAu<sub>5</sub>In-3". Models 3 and 4 are constructed of two "EuAu<sub>4+x</sub>In<sub>2−x</sub>" segments to accomplish broader options for structural variations.

perpendicular to the stacking direction within one segment.<sup>64</sup> In the orthorhombic structure the neighboring layers of the three succeeding "EuAu<sub>4+x</sub>In<sub>2−x</sub>" p[are](#page-9-0)ntal segments  $(3<sup>6</sup>)$  are aligned in opposite directions with a torsion angle of 102.7°, while the "EuAu<sub>4+x</sub>In<sub>2-x</sub>" slabs line up in the same direction in the monoclinic structure (Figure 2). Accordingly, the orthorhombic structure comprises two  $(3^{6}_{1}1^{3}_{2})$  sections in succession and has a longer [translatio](#page-4-0)n period along the stacking direction than the monoclinic compound. The disordered M sites of the orthorhombic structure exhibit larger indium contributions relative to the monoclinic compound and lead to a higher indium content in III than for the monoclinic  $Eu<sub>517.7</sub>In<sub>4.3</sub>.$ 

Coloring and Electronic Structure. An analysis of the electronic structure for the ribbons of the face-sharing Au<sub>8</sub> cages enclosing Eu, Au, and In atoms was accomplished for the tetragonal structures, which show the shortest repeat unit along (001) within the series  $EuAu_{4.8}In_{1.2}$ ,  $Eu_5Au_{17.7}In_{4.3}$ , and  $Eu<sub>5</sub>Au<sub>17.3</sub>In<sub>4.7</sub>$ . To understand the site preference for the mixed Au/In occupancy on the Wyckoff position 4d different starting models were examined (see Computational Details): an ordered "EuAu<sub>4</sub>In<sub>2</sub>" model that is derived from the tetragonal structures through full indium occu[pations of the mixed M](#page-2-0) sites and diverse "EuAu<sub>5</sub>In" models with mixed Au/In occupations on both the 8h (models 1 and 2) and the 4d (models 3 and 4)

sites, respectively (Figure 3). The diverse "EuAu<sub>5</sub>In" models were inspected to reveal the influence of dissimilar heteroatomic Au−In bond frequencies and different local atomic environments on the arrangements of gold and indium in the tetragonal structures. In intermetallic compounds with disordered networks the model with the maximal number of heteroatomic contacts tends to provide the lowest total energy and is typically expected to be the most favorable scheme to compare to the experimental structure.<sup>65−67</sup> To examine a likely presence of this tendency for the tetragonal compounds, schemes with maximal numbers of [hetero](#page-9-0)atomic Au−In contacts have been achieved for the gold and indium distributions in models 1 and 3, which resemble Au/In partitioning on the 8h and 4d sites of the observed structure, respectively. The Au/In distributions in "EuAu<sub>5</sub>In" models 2 and 4 give slightly lower amounts of Au−In contacts relative to "EuAu<sub>5</sub>In-1 and -3", respectively, to develop tendencies between the bond frequencies, local atomic environments, and bond as well as total energies for this series. The outcome of this analysis will help to understand the site preferences for this particular system and to corroborate the experimentally determined structure as the electronically most favorable.

A topological analysis of the tetragonal structure reveals that an indium occupation of the 8h site brings about a maximum of 8 heteroatomic Au−In contacts per indium atom, while placing

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Figure 4. DOS (left) and −COHP curves (right) of the "EuAu<sub>4</sub>In<sub>"</sub> and "EuAu<sub>3</sub>In" models computed by the TB-LMTO method: the Fermi level is represented by the dashed lines, while orbital-projected DOS curves of both models may be extracted from the Supporting Information (Figure S9). Optimized structural parameters of the "EuAu<sub>5</sub>In" model 3, which is the "EuAu<sub>5</sub>In" composition with the lowest total energy, were used as starting points for the TB-LMTO-based calculations. Spin-polarized DOS curves (VASP) are provided in Figure S8, [Supporting Information.](#page-8-0)

indium on the Wyckoff position 4d leads to a maximum of 10 Au−In contacts/In. Accordingly, higher Au−In bond frequencies are achieved for all M−M contacts in models 3 and 4, in which the indium atoms reside on the positions 4d, rather than for models 1 and 2 with In atoms occupying the 8h sites (Figure 3). Because the scheme with the maximal number of heteroatomic contacts tends to give the lowest total energies for s[tructures](#page-5-0) with disordered networks,<sup>68</sup> one would expect the model with the lowest homoatomic bond frequency to be the most favorable to compare to the [exp](#page-9-0)erimental structure. A comparison of the total energies for the "EuAu<sub>5</sub>In" models indicates that the lowest total energy is obtained for model 3, which is the scheme with the largest number of Au−In contacts per indium atom, and provides justification why indium prefers to occupy the 4d rather than the 8h sites.

Because preliminary calculations with varying correlation parameters (Figure S7, Supporting Information) indicated strong correlations for the Eu  $4f$  states,<sup>69-71</sup> an effective on-site Coulomb interaction term ( $U_{\text{eff}}$  [= 3 eV\) was inc](#page-8-0)luded as a correctional parameter to the Kohn−S[ham](#page-9-0) Hamiltonian of the spin-polarized calculations. The total energy calculations on a ferromagnetic and an antiferromagnetic "EuAu<sub>4</sub>In<sub>2</sub>" model revealed an energy difference of 8.2 meV/cell between the antiferromagnetic and the lower lying ferromagnetic state, which tends to be preferred in fair agreement with the magnetic data.<sup>72</sup> The spin-polarized DOS curves of "EuAu<sub>4</sub>In<sub>2</sub>" (Figure S8, Supporting Information) do not superimpose, inferring a ferr[om](#page-9-0)agnetic state with a major difference for the Eu 4f states as t[he origin of a magnetic](#page-8-0) response.<sup>72</sup> The bands accounting for the Eu 4f AOs exhibit extremely small dispersions leading to sharp peaks at 4.22 and 11.72 eV in t[he](#page-9-0) spin-up and spin-down DOS curves, respectively. Such small dispersions are indicative of rather localized states playing a subordinate role in overall bonding and provide justification to treat the Eu 4f AOs as core-like states in the LMTO-based calculations.

Density of States. To p[rovide insight into the](#page-8-0) electronic structures of the disordered tetragonal compositions Eu-Au<sub>4+x</sub>In<sub>2−x</sub> (x = 0.8−1.0), which lie between those of the ordered "EuAu<sub>4</sub>In<sub>2</sub>" and "EuAu<sub>5</sub>In", we followed up with an analysis of the DOS curves (Figure 4) for the "EuAu<sub>4</sub>In<sub>2</sub>" and the lowest energy "EuAu<sub>5</sub>In" models. A comparison of the DOS curves for both models reveals significant contributions from the Au-d atomic orbitals (AOs), which mainly reside between  $-6.30$  and  $-2.18$  eV for "EuAu<sub>4</sub>In<sub>2</sub>" and between  $-6.57$  and  $-2.01$  eV for "EuAu<sub>5</sub>In". The states near the Fermi level,  $E_F$ , originate primarily from the Au-d states with minor contributions from the Eu-d and In-p AOs, respectively. An analysis of the VASP-based DOS curves for a hypothetical model of "Eu<sub>5</sub>Au<sub>16</sub>In<sub>6</sub>", which is derived from the orthorhombic structure of III through assignments of the major component indium on the disordered M sites (Wyckoff positions 8f, 8f, 8f), reveals alike tendencies (Figure S10, Supporting Information). In particular, the states below  $E_F$  arise mainly from the Au-d AOs (between −2.33 and 2.32 eV), [whereas the states aroun](#page-8-0)d the Fermi level stem mostly from the bands accounting for the Au-d AOs with minor shares from the Eu-d and In-p states, respectively. Because the refined composition of III has 41.4 valence electrons per formula unit (VEs/fu) and the composition of "Eu<sub>5</sub>Au<sub>16</sub>In<sub>6</sub>" corresponds to 44 VEs/fu, it is rather inapt to evaluate stability tendencies for the  $Eu<sub>5</sub>Au<sub>16</sub>(Au/In)<sub>6</sub>$  structures based on the relative position of the Fermi level in "Eu<sub>5</sub>Au<sub>16</sub>In<sub>6</sub>"; however,  $E_F$  in "Eu<sub>5</sub>Au<sub>16</sub>In<sub>6</sub>" falls in a deep pseudogap, indicating an electronically favorable situation.

Notwithstanding that the general features are similar for "EuAu<sub>4</sub>In<sub>2</sub>" and "EuAu<sub>5</sub>In", still, the models differ in both composition and valence electron counts (vec). The Fermi level in "EuAu<sub>4</sub>In<sub>2</sub>" (12 valence electrons) falls close to a local maximum in the DOS curve, while  $E_F$  in "EuAu<sub>5</sub>In" (10 valence electrons) falls in a pseudogap that is generated in the DOS regions for vec of 9.9−10.6 VEs/fu. As the tetragonal structure

<span id="page-7-0"></span>Table 3. Distance and −ICOHP/Bond Ranges, Average −ICOHP/Bond, Cumulative −ICOHP/Cell, and Percentage<br>Contributions of the Diverse Interactions in "EuAu In." "EuAu In-1" "EuAu In-2" "EuAu In-3" and "EuAu In-4"" Contributions of the Diverse Interactions in "EuAu<sub>4</sub>In<sub>2</sub>", "EuAu<sub>5</sub>In-1", "EuAu<sub>5</sub>In-2", "EuAu<sub>5</sub>In-3", and "EuAu<sub>5</sub>In-4"



II refines as  $EuAu_{4.75}In_{1.25(2)}$ , which corresponds to 10.5 VEs/ fu, the Fermi level will be located near the higher part of the pseudogap in the "EuAu<sub>5</sub>In" DOS. Likewise,  $E_F$  in EuAu<sub>4.93</sub>In<sub>1.07(2)</sub> (10.1 VEs/fu) and EuAu<sub>5.03</sub>In<sub>0.97(2)</sub> (9.9 VEs/ fu) will occur near higher and lower parts of the pseudogap, respectively. This result alludes to a higher relevance of valence electron concentrations toward distributing gold and indium sites.

In summary, the total energy calculations point to a site preference of the 4d sites for the Au/In partitioning in the tetragonal structures. On the basis of an analysis of the DOS curves for both "EuAu<sub>4</sub>In<sub>2</sub>" and "EuAu<sub>5</sub>In" valence electron concentrations appear to play a relevant role in these structures. Another important contribution that one would expect to influence the assignments of elements on intrinsic positions within one structure is the bond energy.<sup>73</sup> To analyze its impact on the tetragonal structure in more detail, we followed up with a (chemical) bonding analysis on [t](#page-9-0)he "EuAu<sub>4</sub>In<sub>2</sub>" and "EuAu<sub>s</sub>In-3" models.

Bonding Analysis. Analysis of the −COHP curves (Figure 4) and their integrated values (Table 3) for both "EuAu<sub>4</sub>In<sub>2</sub>" and "EuAu<sub>5</sub>In" model-3 indicates that significant b[onding](#page-6-0) [in](#page-6-0)teractions are evident for the homoatomic M−M as well as the heteroatomic Au−In contacts. A direct comparison between the −ICOHP values of both systems cannot be made as the average electrostatic potential in each DFT-based calculations is scaled to an arbitrary "zero" energy; $74$  however, projecting −ICOHP values weighted by bond frequencies as percentages to the total bonding capacities has [be](#page-9-0)en demonstrated to provide conclusive hints to the bonding differences between dissimilar structures. 53,54,75

The Au−Au −ICOHP values range [from 0.8351 to 0.77](#page-8-0)65 eV/bond for "EuAu<sub>4</sub>In<sub>2</sub>" and from 1.0112 to 0.6365 eV/bond for the more Au-rich composition and contribute 32.82% and 57.05% to the total bonding of the respective structures. Note that the percentage contribution of the Au−Au contacts is larger in "EuAu<sub>5</sub>In" than in the more In-rich structure as a consequence of the higher Au−Au bond frequencies in "EuAu5In". Because −ICOHP values tend to scale similarly to bond strength, generally, the magnitude of the −ICOHP values will decrease as the bond lengths increase. For example, the largest Au-Au -ICOHP value of the ordered "EuAu<sub>4</sub>In<sub>2</sub>"  $(0.8351 \text{ eV/bond})$  occurs for the separations  $(d = 2.853 \text{ Å})$  that enclose the squared bases of the  $Au_8$  cages within the *ab* plane, while the Au−Au separations in the zigzag chains between these Au<sub>4</sub> squares are 3.071 Å and have an  $-ICOHP$  value of 0.7765 eV/bond. The homoatomic Au−Au interactions are optimized at  $-1.18$  eV for "EuAu<sub>4</sub>In<sub>2</sub>" and at  $-1.58$  eV for "EuAu<sub>5</sub>In" and remain nonbonding until  $E<sub>F</sub>$ . The strongly antibonding Au−Au interactions at around −3.26 eV for "EuAu<sub>4</sub>In<sub>2</sub>" and  $-3.05$  eV for "EuAu<sub>5</sub>In" stem from the repulsions of the Au-d orbitals, which are observed typically for gold-rich intermetallic compounds.<sup>76</sup>

The heteroatomic Au−In contacts are nonbonding around  $E_F$  (between -0.90 and 0.39 eV f[or](#page-9-0) "EuAu<sub>4</sub>In<sub>2</sub>" and between −0.44 and 1.55 eV for "EuAu<sub>5</sub>In") and change to antibonding states at 0.39 eV for "EuAu<sub>4</sub>In<sub>2</sub>" and at 1.55 eV for "EuAu<sub>5</sub>In". These interactions contribute 51.54% and 36.45% to the total bonding of "EuAu<sub>4</sub>In<sub>2</sub>" and "EuAu<sub>5</sub>In-3", respectively. The difference in the percentage contributions of the Au−In contacts to the total bonding capacities originates from the dissimilar bond frequencies between "EuAu<sub>5</sub>In" and "Eu-Au4In2", which has twice as many Au−In as Au−Au contacts.

<span id="page-8-0"></span>Another significant difference between the "EuAu<sub>4</sub>In<sub>2</sub>" and the "EuAu<sub>5</sub>In" models is the absence of any close, homoatomic In-In contacts between the face-sharing  $M(\partial A)u_8$  cages in the latter structure. These contacts  $(d = 2.840 \text{ Å})$  are evident for the ordered "EuAu<sub>4</sub>In<sub>2</sub>" and show bonding interactions with an −ICOHP value of 0.8155 eV/bond; in the more gold-rich model, however, the short Au−In separations (2.794 Å) exhibit strong bonding populations between the  $M(\partial A)u_8$  cages.

A comparison of the Au−Au and Au−In −ICOHP values for the "EuAu<sub>4</sub>In<sub>2</sub>" and the lowest energy "EuAu<sub>5</sub>In" models reveals that these values scale in the same range for the more Au-rich structure but show a significant difference in the ordered "EuAu<sub>4</sub>In<sub>2</sub>" (Table 3). As a consequence, there are strong Au−Au as well as Au−In bonding interactions in "EuAu5In", whereas the −ICOHP values are much smaller for the heteroatomic tha[n](#page-7-0) [for](#page-7-0) [th](#page-7-0)e homoatomic contacts in the ordered "EuAu<sub>4</sub>In<sub>2</sub>". Although bond frequencies are a substantial factor in these structures and for their formations, this result also indicates the influence of the local symmetry and the intrinsic atomic arrangements. This impact comes even clearer from a comparison between "EuAu<sub>5</sub>In" models 1 and 2. Even though model 1 has a higher Au−In bond frequency than model 2, this discrepancy is overcome by the higher amount of strong Au−Au interactions in 2, for which a lower total energy is evaluated rather than for model 1. This outcome suggests that the subtle interplay between Au−In bond frequencies and local atomic environments not only adjusts the site preferences for the Au/In partitioning but also controls the structural preferences for these compounds. The formally anionic networks of the diverse models encapsulate europium atoms, which reside in the centers of two face-sharing  $M_8$  cages. The magnitudes of the M−Eu −ICOHP values are smaller than those for the Au−Au, Au−In, and In−In interactions, which is observed typically for rare-earth late-transition-metal intermetallic compounds.<sup>68</sup>

## ■ C[ON](#page-9-0)CLUSIONS

Exploration of the gold-rich regions for the Eu−Au−In system lead to the discovery of three ternary intermetallic compounds. EuAu<sub>0.46</sub>In<sub>1.54(2)</sub> (I) can be derived from the binary EuAu<sub>2</sub> through partial indium occupation of the Au sites. Significant gold distributions on the indium sites are observed for the "EuAu<sub>4</sub>In<sub>2</sub>"-derived EuAu<sub>4+x</sub>In<sub>2−x</sub> with  $x = 0.75(2)$  (II),  $0.93(2)$ , and  $1.03(2)$ . The mutual exchange of Au and In atoms for these structures while maintaining their host lattices substantiates the mutual exchangeabilities of Au and In but also points to certain electronical flexibilities for I and II. A combination of the structural elements of I and II was realized in Eu<sub>5</sub>Au<sub>17.29</sub>In<sub>4.71(3)</sub> (III), which adopts its own structure type. A topological analysis for the recently reported  $Eu<sub>5</sub>Au<sub>17.7</sub>In<sub>4.3</sub>$ and  $Eu<sub>5</sub>Au<sub>17.29</sub>In<sub>4.71(3)</sub> (III) reveals that these compounds$ formally represent one-dimensional intergrowths of the series EuAu<sub>2</sub>−"EuAu<sub>4+x</sub>In<sub>2−x</sub>".

The electronic structure was examined for the EuAu<sub>4+x</sub>In<sub>2−x</sub> compounds, which show the shortest repeat unit along (001) within the reported series. Electronic structure calculations on diverse "EuAu<sub>5</sub>In" models indicated that there are clear site preferences of mixing indium on the 4d site rather than the 8h sites. From a topological analysis it becomes clear that this tendency arises from the attempt to optimize the frequency of the heteroatomic Au−In bonds, which is achieved through partial occupation of the 4d sites by indium. The positions of the Fermi level in the DOS of the "EuAu<sub>4</sub>In<sub>2</sub>" and the lowest

energy "EuAu<sub>5</sub>In" models reveal electronically favorable situations for the tetragonal structures but also suggest that valence electron concentrations are of higher relevance for their formations. On the basis of a chemical bonding analysis it is the subtle interplay between the heteroatomic bond frequencies and the approach to sustain strong local atomic contacts that ascertains the adaption of an intrinsic structure for this system.

## ■ ASSOCIATED CONTENT

#### **S** Supporting Information

Tables of the atomic anisotropic displacement parameters for I, II, and III; simulated and measured PXRD patterns of I, II, and III; representations of the miscellaneous coordination environments in II and III; spin-polarized (VASP) and TB-LMTObased DOS data for "EuAu<sub>4</sub>In<sub>2</sub>" and the lowest energy "EuAu5In" model; distances, multiplicities and −ICOHP/ bond values for selected interactions in "EuAu<sub>4</sub>In<sub>2</sub>" and all "EuAu<sub>5</sub>In" models; DOS and projected DOS curves (VASP) of a hypothetical composition "Eu<sub>5</sub>Au<sub>16</sub>In<sub>6</sub>"; crystallographic information on the ternary EuAu<sub>0.46</sub>In<sub>1.54(2)</sub> (I), EuAu<sub>4+x</sub>In<sub>2-x</sub>  $(x = 0.75(2)$  (II),  $0.93(2)$ ,  $1.03(2)$ ) and  $Eu<sub>5</sub>Au<sub>17.29</sub>In<sub>4.71(3)</sub>$  (III) in cif form; The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/ acs.inorgchem.5b00257.

### ■ [AUTHOR INFOR](http://pubs.acs.org/doi/abs/10.1021/acs.inorgchem.5b00257)[MATION](http://pubs.acs.org)

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#### Notes

The auth[ors declare no compe](mailto:mudring@iastate.edu)ting financial interest.

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